This is a list of all substantial corrections made to Computers \＆Typesetting between the publication of the second＂Millennium Edition＂at the close of the year 2001 and the beginning of the year 2014．（More precisely，it lists errors corrected in 16th to 19 th printings of Volume A，the 7 th and 8 th printings of Volume B，the 6th and 7th printings of Volume C，the 4th and 5th printings of Volume D，and the 5th and 6th printings of Volume E．）Corrections made to the softcover version of The $T_{E} X b o o k$ ，beginning with its 32 nd printing，are the same as corrections to Volume A．Corrections to the softcover version of The METAFONTbook，beginning with its 11th printing，are the same as corrections to Volume C．Changes to the mini－indexes and master indexes of Volumes B，D， and E are not shown here unless they are not obviously derivable from what has been shown．All of these errors have supposedly been corrected in more recent printings，unless they were subsequently found to be wrong．

Page A7，line 4 from the bottom（01／15／04）
since control sequences of the second kind always have exactly one symbol after

## Page A123，line 7 from the bottom

（02／27／08）
that it won＇t make the natural height－plus－depth of $\backslash$ box $n$ surpass \dimen $n$ ，when it is
Page A124，lines 12 and 13
（02／27／08）
means that $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ has tried to split an \insert254 to height 180.2 pt ；the natural height－ plus－depth of the best such split is 175.3 pt ，and the penalty for breaking there is 100 ．）

Page A153，line 7
（01／03／14）
of three fonts：one for text size，one for script size，and one for scriptscript size．The
Page A206，lines 12－17
（05／21／07）
or alignment template is also considered to be \outer in this sense；for example，a file shouldn＇t end in the middle of a definition．If you are designing a format for others to use，you can help them detect errors before too much harm is done，by using \outer with all control sequences that should appear only at＂quiet times＂within a document． For example，Appendix B defines \proclaim to be \outer，since a user shouldn＇t be stating a theorem as part of a definition or argument or preamble．

Page A216，line 3 from the bottom
$(12 / 20 / 07)$
\openin〈number〉＝〈file name〉
Page A290，lines 25－26
$(02 / 24 / 08)$
－$\langle$ leaders $\rangle\langle$ box or rule $\rangle\langle$ horizontal skip $\rangle$ ．Here $\langle$ horizontal skip $\rangle$ refers to one of the first five glue－appending commands just mentioned；the formal syntax for 〈leaders〉

Page A292, line 15
(12/02/02)
are defined as in the second alternative of a 〈math field〉, are recorded in a "choice
Page A308, lines 25 and 26
(06/17/02)
\def \appendroman\#1\#2\#3\{\expandafter\def $\backslash$ expandafter\#1\expandafter \{\csname\expandafter\gobble\string\#2\romannumeral\#3\endcsname\}\}

Page A311, line 14 (12/02/02)
$\backslash d e f \backslash \backslash\{\backslash i f \backslash$ space $\backslash n e x t \backslash \%$ assume that $\backslash$ next is unexpandable
Page A311, line 17 (12/29/07)
\leavevmode\copy0\kern-\wdO\makelightbox\}
Page A318, lines 24 and 25
(10/01/03)
15.13. Yes, in severe circumstances. (1) Previous footnotes might have left no room for any more footnotes on the page. (2) If \vadjust $\{\backslash$ eject $\}$ occurs on the same line

```
Page A364, lines 12-15 from the bottom
(02/29/08)
\def\loggingall{\tracingcommands=2 \tracingstats=2
    \tracingpages=1 \tracingoutput=1 \tracinglostchars=1
    \tracingmacros=2 \tracingparagraphs=1 \tracingrestores=1
    \showboxbreadth=\maxdimen \showboxdepth=\maxdimen}
\def\tracingall{\tracingonline=1 \loggingall}
```

Page A364, line 5 from the bottom

Page A373, lines 4 and 5 from the bottom
(01/02/14)
And here's another solution (which may be faster, because token list registers can be expanded more quickly than macros on some implementations, using \the):

Page A399, line 18, through what used to be page A400, line $14 \quad(02 / 26 / 08)$
Finally, the reformatting of \box $\backslash$ footins can be achieved easily with an elegant technique suggested by David Kastrup, using the following $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ code within the \output routine:

```
\def\makefootnoteparagraph{\unvbox\footins
    \baselineskip=\footnotebaselineskip \removehboxes}
\def\removehboxes{\unskip\setbox0=\lastbox
    \ifhbox0{\removehboxes}\unhbox0 \else\noindent \fi}
```

The key idea here is \removehboxes, a macro that has the magical ability to take a vertical box such as ' $\backslash$ vbox\{ $\backslash$ box $1 \backslash$ box $2 \backslash$ box $3 \backslash$ removehboxes $\}$ ' and transform it into ' \vbox\{\noindent \unhbox1 \unhbox2\unhbox3\}', if \box1, \box2, and \box3 are hboxes. Notice how \removehboxes introduces braces so that $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ 's save stack will hold all of the hboxes before they are unboxed. Each level of recursion in this routine uses one cell of input stack space and three cells of save stack space; thus, it is generally safe to do more than 100 footnotes without exceeding $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ 's capacity.

In our application there is no interline glue within \box $\backslash$ footins, so the \unskip command could be deleted from \removehboxes.

Incidentally, the \unskip and \lastbox operations have running times of the approximate form $a+m b$, where $m$ is the number of items on the list preceding the glue or box that is removed. Hence $\backslash$ removehboxes has a running time of order $n^{2}$ when it removes $n$ boxes. But the constant $b$ is so small that for practical purposes it's possible to think of \unskip and \lastbox as almost instantaneous.

Page A416, lines 18-22
(06/08/07)
\def \leftheadline\{\hbox to \pagewidth\{\spaceskip=0pt
\vbox to 10pt\{\}\% strut to position the baseline
$\backslash l l a p\{\backslash t e n b f \backslash f o l i o \backslash k e r n 1 p c\} \%$ folio to left of text
\tenit\rhead\hfil\}\} \% running head flush left
$\backslash d e f \backslash r i g h t h e a d l i n e\{\backslash h b o x$ to $\backslash$ pagewidth\{\spaceskip=0pt\vbox to 10pt\{\}\%

Page A418, line 8 from the bottom
(12/13/11)
$\backslash \operatorname{def} \backslash \backslash\{\# 3\}$ \advance $\backslash$ hsize by -18 mm

Page A418, line 3 from the bottom
(12/13/11)
\halign\{\line\{\titlefont\hss\#\#\}<br>\#\#4unskip<br>\}
$\overline{\text { Page A442, lines } 7 \text { and } 8 \text { from the bottom (01/03/14) }}$
3. If the current item is a style change, set $C$ to the specified style and move on to the next item.
$s_{1}$ tic ${ }_{1} \exp \mathrm{x}_{3} \mathrm{p} \mathrm{pi}_{3} \mathrm{a}{ }_{2} \mathrm{i}_{1} \mathrm{a} \mathrm{i}_{2}$ al ${ }_{2}$ id ${ }_{1}$ do ${ }_{1} \mathrm{ci}{ }_{2}$ io ou ${ }_{2}$ us
(where subscripts that aren't shown are zero), and this yields

$\overline{\text { Page A458, left column }}$
<br>, 38, 356, 378, 418.
Page A459, left column (03/17/06)
angle brackets ( $\rangle$ ), 59, 146-147, 150, 156,
$\underline{268}, 420,437$; see also \langle, \rangle.
Page A461, left column
(02/24/08)
\boxit, 223, 331.
Page A468, right column $\quad(02 / 26 / 08)$
interline glue, $78-79, \underline{80}, 104,105,125,221$,
$245,263,281-282,335,352,399,409$.
Page A469, left column
(02/26/08)
Kastrup, David Friedrich, 399.
Page A470, left column
(01/21/03)
\loggingall, 364.
Page A477, right column (06/08/07)
*\spaceskip, 76, 274, 317, 356, 416, 429.
$\overline{\text { Page A479, right column }} \quad(09 / 11 / 07)$
\undefined, 350, 384.
Page A483, line 5 from the bottom (11/18/03)

- HIERONYMUS HORNSCHUCH, 'Op७oтv

Page Bv, page number change
(12/27/11)
[For consistency with Volumes A, C, and E, the preface now begins on page v instead of page vii. This change was first made in the ninth printing.]

## Page Bv (formerly Bvii), bottom two lines

(01/06/14)
all of those changes. I now believe that the final bug was discovered on 14 September 2008 and removed in version 3.14159265. The finder's fee has converged to $\$ 327.68$.

Page Bxiii (formerly Bxv), line -7
Format specs have no effect on the corresponding Pascal program, but they do influence

> Page B2, line 10 from the bottom
> (01/02/14)

Page B3, new paragraph to follow line 9
(12/20/02)
Incidentally, Pascal's standard round function can be problematical, because it disagrees with the IEEE floating-point standard. Many implementors have therefore chosen to substitute their own home-grown rounding procedure.

Page B21, lines 33 and 34
(09/11/07)
['41 .. '46, '60 .. '71, '136, '141 .. '146, '160 .. '171] must be printable. Thus, at least 81 printable characters are needed.

## Page B109, line 16

(01/06/14)
begin print_esc("csname"); print_esc("endcsname"); print_char(" "); end
Page B114, line $25 \quad(09 / 11 / 07)$
define save_index $(\#) \equiv$ save_stack[\#].hh.rh $\quad$ \{ eqtb location or token or save_stack location \}
Page B139, line 20
(12/19/02)
begin while $($ state $=$ token_list $) \wedge($ loc $=$ null $) \wedge\left(\right.$ token_type $\neq v_{-}$template $)$do end_token_list; $\quad$ \{ conserve stack space $\}$

Page B144, line 14
(09/11/07)
cat: 0 .. max_char_code; $\{$ cat_code(cur_char), usually \}
Page B153, lines 2 and 3
(09/11/07)
In fact, these three procedures account for almost every use of get_next.
Page B161, line 19
(12/19/02)
while $($ state $=$ token_list $) \wedge(l o c=$ null $) \wedge\left(\right.$ token_type $\neq v_{-}$template $)$do end_token_list; \{ conserve stack space \}
long_state $\leftarrow$ call; cur_tok $\leftarrow$ par_token; ins_error $;$ goto continue;

```
Page B172, lines 2-6 from the bottom
    (09/11/07)
else if \(m=\) vmode then scanned_result(prev_depth)(dimen_val)
    else scanned_result(space_factor)(int_val)
```

Page B178, line 4 (09/11/07)
cur_val $\leftarrow 0$; cur_val_level $\leftarrow$ int_val; radix $\leftarrow 0$; cur_order $\leftarrow$ normal;
Page B184, line 9 from the bottom $\quad(04 / 18 / 07)$
and denominator sum to 32768 or less. According to the definitions here, $2660 \mathrm{dd} \approx 1000.33297 \mathrm{~mm}$;
Page B206, line 14
(10/30/02)
used input files like webmac.tex.

## Page B206, new paragraph to follow line 22

The following procedures don't allow spaces to be part of file names; but some users seem to like names that are spaced-out. System-dependent changes to allow such things should probably be made with reluctance, and only when an entire file name that includes spaces is "quoted" somehow.

| Page B227, new line to precede line 23 | $(09 / 11 / 07)$ |
| :--- | :--- |

if $(n w=0) \vee(n h=0) \vee(n d=0) \vee(n i=0)$ then abort;

```
Page B256, line 25
(12/20/02)
    cur_glue: real; { glue seen so far }
    cur_g: scaled; {rounded equivalent of cur_glue times the glue ratio }
    begin cur_g}\leftarrow0; cur_glue \leftarrow &float_constant(0)
    this_box \leftarrow temp_ptr; g_order }\leftarrow\mathrm{ glue_order(this_box); g_sign }\leftarrow\mathrm{ glue_sign(this_box);
```

Page B258, line 5 from the bottom
(12/20/02)
begin $g \leftarrow$ glue_ptr $(p)$; rule_wd $\leftarrow$ width $(g)-c u r_{-} g$;
Page B258, bottom line
begin cur_glue $\leftarrow$ cur_glue $+\operatorname{stretch}(g)$; vet_glue $\left(f l o a t\left(g l u e \_s e t\left(t h i s \_b o x\right)\right) *\right.$ cur_glue $)$;
cur_g $\leftarrow$ round (glue_temp);
Page B259, line 4
begin cur_glue $\leftarrow$ cur_glue $-\operatorname{shrink}(g)$; vet_glue $\left(\right.$ float $\left(g l u e_{-} s e t\left(t h i s \_b o x\right)\right) *$ cur_glue);
cur_ $g \leftarrow$ round (glue_temp);
Page B259, new line to precede old line 7
(12/20/02)
$r u l e \_w d \leftarrow r u l e_{-} w d+c u r_{-} g ;$

## Page B260, line 21

(12/19/02)
else begin $l x \leftarrow l r \operatorname{div}(l q+1) ;$
Page B261, line 9
(12/20/02)
cur_glue: real; \{glue seen so far \}
cur_g: scaled; \{rounded equivalent of cur_glue times the glue ratio \}
begin cur_ $g \leftarrow 0$; cur_glue $\leftarrow$ float_constant $(0)$;
this_box $\leftarrow$ temp_ptr $;$ g_order $\leftarrow$ glue_order $($ this_box $) ;$ g_sign $\leftarrow$ glue_sign(this_box);

## Page B262, line 10 from the bottom

(12/20/02)
begin $g \leftarrow$ glue_ptr $(p)$; rule_ht $\leftarrow$ width $(g)-c u r_{-} g$;
Page B262, line 6 from the bottom (12/20/02)
begin cur_glue $\leftarrow$ cur_glue $+\operatorname{stretch}(g)$; vet_glue $\left(f l o a t\left(g l u e \_s e t\left(t h i s \_b o x\right)\right) *\right.$ cur_glue);
cur_g $\leftarrow$ round (glue_temp);

## Page B262, line 2 from the bottom

begin cur_glue $\leftarrow$ cur_glue $-\operatorname{shrink}(g)$; vet_glue $\left(f l o a t\left(g l u e_{-} s e t\left(t h i s \_b o x\right)\right) *\right.$ cur_glue $)$;
cur_g $\leftarrow$ round (glue_temp);
Page B263, new line to precede old line 2
(12/20/02)
$r u l e_{-} h t \leftarrow r u l e_{-} h t+c u r_{-} g ;$
Page B264, line 10
(12/19/02)
else begin $l x \leftarrow l r \operatorname{div}(l q+1)$;
Page B266, line 29
(09/11/07)
total_pages $\geq 65536$, the DVI file will lie. And if max_push $\geq 65536$, the user deserves whatever chaos might ensue.

Page B279, line 19
(09/11/07)
$p:$ pointer; $\{$ a new glue node $\}$
Page B288, lines 18-20
(09/11/07)
left_noad: begin print_esc("left"); print_delimiter(delimiter $(p)$ ); end;
right_noad: begin print_esc("right"); print_delimiter(delimiter(p));
Page B290, line 12 (09/11/07)
begin if $s=$ text_size then print_esc("textfont");

Page B299, line 9
if type $(r)=$ kern_node then $\quad\{$ unneeded italic correction $\}$
Page B332, line 6
(12/19/02)
is being scanned, or when no alignment preamble is active.
Page B332, line 8
(12/19/02)
begin if $($ scanner_status $=$ aligning $) \vee($ cur_align $=$ null $)$ then
Page B336, line 11 from the bottom
(10/13/03)
$j-i+$ min_quarterword in their link fields. The values of $w_{i i}$ were initialized to null_flag,
Page B342, lines 5 and 6
(09/11/07)
In restricted horizontal mode, the clang part of aux is undefined; an over-cautious Pascal runtime system may complain about this.

$$
\begin{array}{ll}
\hline \text { Page B343, line } 25 & (01 / 02 / 13) \\
\hline
\end{array}
$$

should begin in the sequence of line numbers, in case hanging indentation or \parshape is in
Page B416, line 22
(02/29/08)
if $\operatorname{count}(t)=1000$ then $t \leftarrow \operatorname{height}(r)$
else $t \leftarrow x$ _over_n $($ height $(r), 1000) *$ count $(t)$;
print_scaled ( $t$ )
Page B438, lines 1-3
(09/11/07)
1035. If $\operatorname{link}\left(c u r_{-} q\right)$ is nonnull when wrapup is invoked, cur $q$ points to the list of characters that were consumed while building the ligature character cur_l.

Page B438, lines 19 and 20
(09/11/07)
begin if $\operatorname{link}\left(\right.$ cur_q $\left._{-}\right)>$null then
if character $($ tail $)=$ qi $($ hyphen_char $[$ main_f $])$ then ins_disc $\leftarrow$ true;

| Page B438, line 4 from the bottom | $(09 / 11 / 07)$ |  |
| :---: | :--- | :---: |
| link $($ tail $) \leftarrow$ lig_stack $;$ tail $\leftarrow$ lig_stack | $\{$ main_loop_lookahead is next $\}$ |  |


| Page B439, line 3 | $(09 / 11 / 07)$ |
| :--- | :--- |

if main_p $>$ null then tail_append $($ main_p $) ; \quad\{$ append a single character $\}$

| Page B440, new line to follow line 9 | $(09 / 11 / 07)$ |
| :--- | :--- |

if cur_r $=$ non_char then goto main_loop_wrapup;

## Page B452, line 18

(28/03/11)
hmode, where the latter two are used to denote \vbox and \hbox, respectively.
$\frac{\text { Page B455, lines } 3 \text { and } 4}{\text { if }\left(\left(c u r_{-} c m d=h s k i p\right) \wedge(\text { abs }(\text { mode }) \neq v \text { mode })\right) \vee\left(\left(c u r_{-} c m d=v s k i p\right) \wedge(\text { abs }(\text { mode })=v m o d e)\right) \text { then }}$

Page B472, new paragraph to follow line 10
A devious user might force an endv command to occur just about anywhere; we must defeat such hacks.

```
Page B472, replacement for what used to be line 13
    begin base_ptr \(\leftarrow\) input_ptr; input_stack[base_ptr] \(\leftarrow\) cur_input;
    while (input_stack[base_ptr].index_field \(\neq v_{-}\)_template) \(\wedge\)
        \((\) input_stack[base_ptr].loc_field \(=\) null \() \wedge\)
        (input_stack[base_ptr].state_field \(=\) token_list \()\) do decr \((\) base_ptr \()\);
    if (input_stack[base_ptr].index_field \(\neq \boldsymbol{v}_{-}\)template) \(\vee\)
        (input_stack \([\) base_ptr].loc_field \(\neq\) null \() \vee\)
        (input_stack \([\) base_ptr].state_field \(\neq\) token_list) then
```



```
    if cur_group \(=\) align_group then
```

(12/20/02)
Page B505, line 19
(09/11/07)

if $p \geq$ glue_val then delete_glue_ref (cur_val);
error; return;
Page B506, line 1
(10/13/03)
1237. Here we use the fact that the consecutive codes int_val .. mu_val and assign_int ..

## Page B520, line 8

(06/25/04)
says, for example, '(preloaded format=plain 1982.11.19)', showing the year, month, and day
Page B535, new line to follow line $11 \quad(09 / 11 / 07)$
if last_glue $\neq$ max_halfword then delete_glue_ref (last_glue);
Page B578, new entry $\quad(06 / 04 / 06)$

Trabb Pardo, Luis Isidoro, 2.

| Page Cxi, line 4 |  | $(05 / 20 / 07)$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2 7}$ | Recovery from Errors | . . . . . . . . . 223 |

Page C11, line 11
(10/11/01)
the area below the bar to the area above it equal to $(\sqrt{5}+1) / 2 \approx 1.61803$, the
Page C29, illustration for exercise 4.11
(09/09/01)
[points 2 and 5 should not be labeled twice]

| Page C32, line 5 from the bottom |
| :---: |
| $20 \quad$ penpos1 (stem, 15) ; penpos2(.9stem, 12) ; penpos3(stem, 10) ; |

## Page C36, line 5 from the bottom

(01/05/14)
line 12 , where it says ' $x 11$ ', not ' x 11 ' or ' xll '); be sure to distinguish between
$\overline{\text { Page C55, lines } 5 \text { and } 6} \quad(01 / 05 / 14)$
suffixed or subscripted. Thus, the syntax rule for $\langle$ variable $\rangle$ should actually be replaced by a slightly more complicated pair of rules:

$$
\begin{array}{rr}
\hline \text { Page C129, line } 16 & (02 / 21 / 08) \\
\langle\text { path subexpression }\rangle \longrightarrow\langle\text { path expression not ending with direction specifier }\rangle
\end{array}
$$

Page C130, lines 13-15 from the bottom
(09/13/03)
point but not after it, the nonempty one is duplicated in a similar way. A basic path join '. . controls $u$ and $v .$. ' specifies explicit control points that override any direction specifiers that may immediately surround it.

Page C137, lines 5-7 from the bottom
(02/21/08)
Let's conclude this chapter by applying what we've learned about paths to a real-life example. The Journal of Algorithms was published for many years by Academic Press, and its cover page carried the following logo, which was designed

## Page C137, bottom two lines

(02/21/08)
A METAFONT program to produce this logo made it possible for the editors of the journal to use it on letterheads in their correspondence. Here is one way to do that job,

Page C156, line 15 from the bottom
(09/09/01)
be the values they had upon entry to the group.)

```
def --- = ..tension infinity.. enddef;
```

it makes＇$z_{1}---z_{2}$＇become＇$z_{1} \ldots$ tension infinity $\ldots z_{2}$＇．The replacement text can be any sequence of tokens not including＇enddef＇；or it can include entire subdefinitions like＇def ．．．enddef＇，according to certain rules that we shall explain later．

Page C171，line 16 from the bottom
（06／18／02）
$\langle$ loop $\rangle \longrightarrow\langle$ loop header $\rangle:\langle$ loop text $\rangle$ endfor
Page C179，line 7 from the bottom（09／09／01）
next time METAFONT gets to the end of an input line，it will stop reading from the
Page C180，lines 14－16
（04／25／03）
digits should be a file name that works in essentially the same way on all installations of METAFONT．Uppercase letters are considered to be distinct from their lowercase counterparts，on many systems．

Page C180，new line to be inserted 4 from the bottom
（06／25／04）
－When METAFONT is reading the symbolic tokens to be saved by save．
$\overline{\text { Page C203，line } 12 \text { from the bottom } \quad(04 / 25 / 03)}$
point 3 at the right of the triangle might digitize into a
Page C213，line 26
（02／21／08）
$\langle$ path subexpression $\longrightarrow$ 〈path expression not ending with direction specifier〉

Page C226，line 23
（02／21／08）
following nineteen things will be mentioned：
$\overline{\text { Page C226，new line to be second from the bottom }}$

Page C236，line 7 from the bottom（01／05／14）
7．4．False．After＇newinternal $x$ ；＇you can＇t say＇$x\langle t a g\rangle$＇in a 〈suffix list〉．
Page C246，line 12
（02／21／08）
is performed whenever METAFONT uses the last two alternatives in the definition

Page C250, lines 13 and 14
19.3. Yes, if and only if $n-\frac{1}{2}$ is a nonnegative even integer. (Because ambiguous values are rounded upwards.)

Page C250, line 12 from the bottom $\quad(04 / 25 / 03)$
following 〈boolean primary〉.)
Page C286, line 25
(09/09/01)
problem; it would simply have put ENDFOR into the replacement text of asts, because
Page C289, line 7
(09/09/01)
if if pair $x: x>(0,0)$ else: false fi: A else: B fi.
Page C292, line 10 from the bottom
(09/09/01)
be known by saying 'if known $p-q: p=q$ else: false fi'; transforms could be handled
Page C293, line 5 from the bottom (04/25/03)
given angle $\phi$. We can consider the common angle $\theta$ of $z_{1 r}-z_{1 l}$ and $z_{0 r}-z_{0 l}$ to be
Page C315, line 15 from the bottom
(04/25/03)
' $b$ ' was shipped out.) The second letter, ' $o$ ', is placed in a second little box adjacent
Page C325, bottom line (02/29/08)

- CAROLUS LINNÆUS, Philosophia Botanica (1751)

Page C332, line 4 from the bottom
(04/25/03)
(The proofsheet resolution will be 50 pixels per inch, because cheapo has 200 pixels per
Page C346, left column
(06/18/02)
*: , 169, 171, 317-319.
Page C346, right column (07/09/01)
*angle, 29, 67, 72, 107, 135, 211, 238.
Page C346, right column
(10/04/04)
arccosine, arcsine, arctangent, see angle.
Page C351, right column
(02/21/08)
independent variables, $\underline{81} \underline{-83}, 88,224,226$.

Page C352, right column
(02/29/08)
Linné, Carl von (= Linnæus, Carolus), 325.
Page C355, right column
(02/29/08)
*save, $155-156,160,173,178,180,218$,
236, 244, 296, 299.
Page Dv, page number change
[For consistency with Volumes A, C, and E, the preface now begins on page v instead of page vii. This change was first made in the sixth printing.]

Page Dv (formerly Dvii), bottom two lines (01/06/14)
corporates all of those changes. I now believe that the final bug was discovered on 03 June 2008, and removed in version 2.7182818. The finder's fee has converged to $\$ 327.68$.

Page Dxiii (formerly Dxv), line -7
$(12 / 27 / 11)$
Format specs have no effect on the corresponding Pascal program, but they do influence
Page D2, line $-17 \quad$ (01/03/14)

Page D2, lines 4 and 5 from the bottom
(12/23/02)
types; there are no 'var' parameters, except in the case of files or in the system-dependent paint_row procedure; there are no tag fields on variant records; there are no real variables; no procedures are declared local to other procedures.)

Page D16, new paragraph to follow line 26
(06/25/04)
The first line is special also because it may be read before METAFONT has input a base file. In such cases, normal error messages cannot yet be given. The following code uses concepts that will be explained later. (If the Pascal compiler does not support non-local goto, the statement 'goto final_end' should be replaced by something that quietly terminates the program.)

Page D22, line 26
(09/11/07)
ASCII codes ['60 .. '71, '136, '141 .. '146] must be printable.

## Page D31, line 29

(06/25/04)
This is the only nontrivial goto statement in the whole program. It is used when there is no

Page D42, replacement for lines 8-13
(12/23/02)
Notice that if 64 -bit integer arithmetic were available, we could simply compute $\left(2^{29} * p+q\right)$ $\operatorname{div}(2 * q)$. But when we are restricted to Pascal's 32 -bit arithmetic we must either resort to multiple-precision maneuvering or use a simple but slow iteration. The multiple-precision technique would be about three times faster than the code adopted here, but it would be comparatively long and tricky, involving about sixteen additional multiplications and divisions.

## Page D43, line 20

(12/23/02)
language or 64 -bit substitute is advisable.
Page D44, lines 24-26
(12/23/02)
Once again it is a good idea to use 64 -bit arithmetic if possible; otherwise take_scaled will use more than $2 \%$ of the running time when the Computer Modern fonts are being generated.

Page D58, line 16 from the bottom
(06/25/04)
if $j_{-}$random $=0$ then new_randoms else decr (j_random)
Page D63, line 21
(06/25/04)
Locations of mem between mem_min and mem_top may be dumped as part of preloaded base
Page D75, line $13 \quad(06 / 25 / 04)$
define fi_or_else $=2 \quad\{$ delimiters for conditionals (elseif, else, fi) $\}$

| Page D76, line 5 | $(06 / 25 / 04)$ |
| :--- | :--- | :--- |
| define tupe name $=30 \quad\{$ declare a type (numeric, pair, etc $)\}$ |  |

define type_name $=30 \quad\{$ declare a type (numeric, pair, etc.) $\}$

| Page D77, line 16 | $(06 / 25 / 04)$ |
| :--- | :--- | ---: |
| define lig_kern_token $=76 \quad\left\{\right.$ the operators 'kern' and ' $=:$ ' ' and $^{\prime}=: I^{\prime}$ ', etc. $\}$ |  |

define lig_kern_token $=76 \quad$ \{ the operators 'kern' and ' $=:$ ' and ' $=: 1$ ', etc. $\}$
Page D98, bottom two lines (06/25/04)

They consist of zero or more parameter tokens followed by a code for the type of macro.

METAFONT user assigns a type to a variable like $x 20 a . b$ by saying, for example, 'boolean $x[] a . b$ '.

Page D102, lines 10-16
(06/25/04)
variable that is relevant when no attributes are attached to the parent. The attr_head node has the fields of either a value node, a subscript node, or an attribute node, depending on what the parent would be if it were not structured; but the subscript and attribute fields are ignored, so it effectively contains only the data of a value node. The link field in this special node points to an attribute node whose attr_loc field is zero; the latter node represents a collective subscript '[]' attached to the parent, and its link field points to the first non-special attribute node (or to end_attr if there are none).

Page D102, lines 7 and 8 from the bottom
(06/25/04)
subscr_head (q1) $=q q 1 ; ~ q q$ is a three-word "attribute-as-value" node with type $(q q)=$ numeric_type (assuming that x 5 is numeric, because $q q$ represents ' x[] ' with no further attributes), name_type $(q q)=$ structured_root, $\quad \operatorname{attr} \_l o c(q q)=0, \quad$ parent $(q q)=p$,

Page D103, line 6
(06/25/04)
The value of variable x 20 b appears in node $q q q 2=\operatorname{link}(q q q 1)$, as you can well imagine. Similarly, the value of ' $\mathrm{x} . \mathrm{a}$ ' appears in node $q 2=\operatorname{link}(q 1)$, where $\operatorname{attr}-l o c(q 2)=h(a)$ and $\operatorname{parent}(q 2)=p$.

Page D114, line 12
(06/25/04)
Such save stack entries are generated by save commands.
Page D120, line 3
(06/25/04)
[delete the line 'The code here ...', since the code doesn't use the stated fact]
Page D126, line $10 \quad(06 / 25 / 04)$
If $\theta_{0}$ is supposed to have a given value $E_{0}$, we simply define $C_{0}=1, D_{0}=0$, and $R_{0}=E_{0}$.
Page D138, line 11 from the bottom
(10/26/06)
for the bisected interval are $z_{0}^{\prime}=z_{0}$ and $z_{0}^{\prime \prime}=z_{0}+\left(Z_{1}^{\prime}+Z_{2}^{\prime}+\cdots+Z_{n}^{\prime}\right) / 2^{l+1}$.

| Page D142, line 3 (06/25/04) |
| :--- |

out to hold if and only if $x_{0} \leq x_{1}$ and $x_{2} \leq x_{3}$, and either $x_{1} \leq x_{2}$ or $\left(x_{1}-x_{2}\right)^{2} \leq\left(x_{1}-x_{0}\right)\left(x_{3}-x_{2}\right)$.
Page D142, line 8
(10/26/06)
For example, if we start with $\left(x_{1}-x_{0}, x_{2}-x_{1}, x_{3}-x_{2}\right)=\left(X_{1}, X_{2}, X_{3}\right)=(7,-16,39)$, the
Page D142, lines 21-23
(06/25/04)
monotonic cubic, then $B\left(x_{0}, x_{1}, x_{2}, x_{3} ; \frac{1}{2}\right)$ is always between $.06\left[x_{0}, x_{3}\right]$ and $.94\left[x_{0}, x_{3}\right]$; and it is impossible for $\bar{x}$ to be within $\epsilon$ of such a number. Contradiction! (The constant .06 is actually $(2-\sqrt{3}) / 4$; the worst case occurs for polynomials like $B(0,2-\sqrt{3}, 1-\sqrt{3}, 3 ; t)$.)

## Page D177, line 18

(06/25/04)
cur_x, cur_y: scaled; \{outputs of skew, unskew, and a few other routines \}
Page D182, lines 27-29
(06/25/04)
399. If the segment numbers on the cycle are $t_{1}, t_{2}, \ldots, t_{m}$, and if $m \leq$ max_quarterword, we have $t_{k-1} \leq t_{k}$ except for at most one value of $k$. If there are no exceptions, $f$ will point to $t_{1}$; otherwise it will point to the exceptional $t_{k}$.

| Page D184, line 18 | $(12 / 21 / 02)$ |
| :---: | :--- | :---: |
| chopped: integer; $\{$ positive if data truncated, negative if data dangerously large \} |  |

Page D184, line 25
(12/21/02)
if $($ internal $[$ autorounding $]>0) \wedge($ chopped $=0)$ then $x y_{-}$round;

| Page D184, line 27 | $(12 / 21 / 02)$ |
| :---: | :---: |
| if $($ internal $[$ autorounding $]>$ unity $) \wedge($ chopped $=0)$ then diag_round; |  |

Page D184, line 32
(12/21/02)
if $($ internal $[$ autorounding $] \leq 0) \vee($ chopped $\neq 0)$ then $\operatorname{print\_ spec~}\left(", \sqcup\right.$ after ${ }_{\lrcorner}$subdivision")

```
Page D185, lines 15-19
    define procrustes \((\#) \equiv\) if \(\operatorname{abs}(\#) \geq d \max\) then
            if abs(\#) > max_allowed then
            begin chopped \(\leftarrow 1\);
            if \# > 0 then \# \(\leftarrow\) max_allowed else \# \(\leftarrow-\) max_allowed;
            end
            else if chopped \(=0\) then chopped \(\leftarrow-1\)
```

(12/21/02)
Page D185, old line 22
(12/21/02)
$p \leftarrow$ cur_spec $; k \leftarrow 1 ;$ chopped $\leftarrow 0 ;$ dmax $\leftarrow$ half (max_allowed);

| Page D185, old line 28 | $(12 / 21 / 02)$ |
| :---: | :---: |
| if chopped $>0$ then |  |

Page D196, lines 3-8
(06/25/04)

The first job is to fix things so that $x(t)$ plus the horizontal pen offset is an integer multiple of the current "granularity" when the derivative $x^{\prime}(t)$ crosses through zero. The given cyclic path contains regions where $x^{\prime}(t) \geq 0$ and regions where $x^{\prime}(t) \leq 0$. The quadrant_subdivide routine is called into action before any of the path coordinates have been skewed, but some of them may have been negated. In regions where $x^{\prime}(t) \geq 0$ we have right_type $=$ first_octant or right_type $=$ eighth_octant ; in regions where $x^{\prime}(t) \leq 0$, we have right_type $=$ fifth_octant or right_type $=$ fourth_octant.

Page D196, lines 15 and 16
(06/25/04)
current pen might be unsymmetric in such a way that $x$ coordinates should round differently in different parts of the curve. These considerations imply that round $\left(x_{0}\right)$

## Page D200, line 4

(06/25/04)
and that there are similar ways to address other important offsets.
[Also delete the definitions of north_south_edge, etc., on lines 11-15; those definitions are never used.]
Page D212, line 18 (06/25/04)
at $\left(x_{0}, y_{0}\right)$ and ends at $\left(x_{1}, y_{1}\right)$, it's possible to prove (by induction on the length of the truncated
Page D216, bottom line
(06/25/04)
we list it twice (with coordinates interchanged, so as to make the second octant look like
Page D217, lines 2-10
(06/25/04)
$w_{2} w_{2} w_{2} \mapsto(-5,6)(-5,6)(-5,6)$
as the list of transformed and skewed offsets to use when curves that travel in the second octant. Similarly, we will have

$$
\begin{array}{rlrl}
w_{2} w_{2} w_{2} & \mapsto(7,-6)(7,-6)(7,-6) & & \text { in the third; } \\
w_{2} w_{2} w_{3} w_{3} & \mapsto(-7,1)(-7,1)(-3,2)(-3,2) & \text { in the fourth; } \\
w_{3} w_{3} w_{3} & \mapsto(3,-2)(3,-2)(3,-2) & & \text { in the fifth; } \\
w_{3} w_{3} w_{0} w_{0} & \mapsto(-3,1)(-3,1)(1,0)(1,0) & & \text { in the sixth; } \\
w_{0} w_{0} w_{0} & \mapsto(1,0)(1,0)(1,0) & & \text { in the seventh; } \\
w_{0} w_{0} w_{0} & \mapsto(-1,1)(-1,1)(-1,1) & & \text { in the eighth. }
\end{array}
$$

Page D218, lines 2 and 3
(06/25/04)
count followed by pointers to the eight offset lists, followed by an indication of the pen's range of values.

Page D218, line 15
(06/25/04)
The link field of a pen header node should be null if and only if the pen is a single point.

Page D228, lines 4-7 from the bottom
(06/25/04)
In odd-numbered octants, the numerator and denominator of this fraction will be nonnegative; in even-numbered octants they will both be nonpositive. Furthermore we always have $0=s_{0} \leq$ $s_{1} \leq \cdots \leq s_{n}=\infty$. The goal of offset_prep is to find an offset index $k$ to associate with each cubic, such that the slope $s(t)$ of the cubic satisfies
Page D231, line 7 (06/25/04)
if $a b s(d u) \geq a b s(d v)$ then $\left\{s_{k-1} \leq 1\right.$ or $\left.s_{k} \leq 1\right\}$
Page D231, line 16
(06/25/04)
and return towards $s_{k-1}$ or $s_{k}$, respectively, yielding another solution of $(*)$.
Page D246, line 4 from the bottom
(06/25/04)
dinate fields. Hence, for example, the point $\left(x_{-} \operatorname{coord}(p)-l e f t \_v(q), y_{-} \operatorname{coord}(p)+r i g h t \_u(p)\right)$ also
Page D248, lines 14 and 15
(01/06/14)
the $x$-axis at the point $\left(\left(a^{2}-b^{2}\right) \sin \theta \cos \theta / \rho\right)+i \rho$, where $\rho=\sqrt{(a \sin \theta)^{2}+(b \cos \theta)^{2}}$. It reaches furthest to the right of the $y$-axis at the point $\sigma+i\left(a^{2}-b^{2}\right) \sin \theta \cos \theta / \sigma$, where $\sigma=$

Page D248, line 24
(06/25/04)
else begin beta $\leftarrow$ minor_axis; gamma $\leftarrow$ major_axis; thet $a \leftarrow 0$;
Page D251, line $1 \quad(01 / 06 / 14)$
536. Only the coordinates need to be copied, not the class numbers and other stuff. At this point either $\operatorname{link}(p)$ or $\operatorname{link}(\operatorname{link}(p))$ is null.

Page D251, line 10
(01/06/14)
done1: if $(\operatorname{link}(p) \neq$ null $)$ then free_node $\left(\operatorname{link}(p), k n o t \_n o d e \_s i z e\right) ;$
$\operatorname{link}(p) \leftarrow s$; beta $\leftarrow-y \_\operatorname{coord}(h)$;
Page D256, line 2 from the bottom
(06/25/04)
we have $2^{l} u_{\text {min }}=2^{l} u_{0}+U_{\text {min }}$, etc.; the condition for overlap reduces to
Page D261, line 5
(06/25/04)
tol: integer; \{bound on the uncertainty in the overlap test \}

```
Page D262, lines 26 and 27
    (06/25/04)
    uv\leftarrowuv+int_packets; { switch from l_packets to r_packets }
    decr(cur_tt); xy \leftarrowxy - int_packets; { switch from r_packets to l_packets }
```

```
Page D262, line 11 from the bottom
    (06/25/04)
```

    \(x y \leftarrow x y+\) int_packets \(; \quad\) \{switch from l_packets to \(r_{-}\)packets \(\}\)
    Page D274, line 15 from the bottom $\quad(06 / 25 / 04)$
begin if serial_no > el_gordo - s_scale then
overflow("independent_variables", serial_no div s_scale);
type $(\#) \leftarrow$ independent; serial_no $\leftarrow$ serial_no + s_scale $;$ value $(\#) \leftarrow$ serial_no;
Page D309, line $21 \quad(06 / 25 / 04)$
670. We go to restart instead of to switch, because we might enter token_state after the error

Page D314, line 6 from the bottom
(06/25/04)
macro_def or iteration).


#### Abstract

Page D330, line 1 (06/25/04)


728. A suffix or text parameter will have been scanned as a token list pointed to by cur_exp,

Page D354, lines 15 and 16 from the bottom
(06/25/04)
cur_type $=$ unknown_boolean means that cur_exp points to a capsule node that is in a ring of equivalent booleans whose value has not yet been defined.

Page D354, lines 11 and 12 from the bottom
(06/25/04)
cur_type $=$ unknown_string means that cur_exp points to a capsule node that is in a ring of equivalent strings whose value has not yet been defined.

Page D354, lines 7 and 8 from the bottom
(06/25/04)
cur_type $=$ unknown_pen means that cur_exp points to a capsule node that is in a ring of equivalent pens whose value has not yet been defined.

Page D355, lines 1 and 2
(06/25/04)
cur_type $=$ unknown_path means that cur_exp points to a capsule node that is in a ring of equivalent paths whose value has not yet been defined.

Page D355, lines 5 and 6
(06/25/04)
cur_type $=$ unknown_picture means that cur_exp points to a capsule node that is in a ring of equivalent pictures whose value has not yet been defined.

Page D355, lines 21 and 22
(06/25/04)
cur_type $=$ token_list means that cur_exp points to a linked list of tokens.

Page D356, lines 2-3
(06/25/04)
nodes have name_type = capsule, and their type field is one of the possibilities for cur_type listed above. Also link $\leq$ void in capsules that aren't part of a token list.

Page D368, line 13
(06/25/04)
my_var_flag: 0 .. max_command_code; $\quad$ initial value of var_flag \}
Page D378, line 9 from the bottom
(06/25/04)
begin cur_type $\leftarrow$ known $;$ cur_exp $\leftarrow 0$; free_node ( $q$, dep_node_size);
Page D380, line 12
(06/25/04)
begin type $(r) \leftarrow$ known; value $(r) \leftarrow 0$; free_node $(p$, dep_node_size $)$;
Page D390, lines 2 and 3
(06/25/04)
by a previous operation. We must maintain the value of right_type $(q)$ in cases such as '. . \{curl2\}z\{0,0<br>$..'. }$

Page D437, line $1 \quad(06 / 25 / 04)$
996. And do_assignment is similar to do_equation:

Page D439, line 10 becomes two lines
(06/25/04)
begin nonlinear_eq ( $v$, cur_exp,false); cur_type $\leftarrow t$; goto done;

| Page D443, line 11 | $(06 / 25 / 04)$ |
| :--- | :--- |

done: if eq_type $(x)$ mod outer_tag $\neq$ tag_token then clear_symbol ( $x$, false $)$;
Page D452, line 9 (06/25/04)
though they don't necessarily correspond to primitive tokens.

| Page D476, line 12 from the bottom | $(06 / 25 / 04)$ |
| :--- | :---: |
| if $n l-$ skip_table $[c]>128$ then |  |

Page D483, line 7
(06/25/04)
max_tfm_dimen $\leftarrow 16 *$ internal [design_size] - $1-$ internal [design_size] div '10000000;
Page D483, lines 15-17 (06/25/04)
if $x>0$ then $x \leftarrow$ max_tfm_dimen else $x \leftarrow-$ max_tfm_dimen; end;
$x \leftarrow$ make_scaled $(x * 16$, internal [design_size] $)$;

Page D496, line 2
(06/25/04)
a pointer to an edge structure. Its mission is to describe the positive pixels in GF form,
Page D500, line 16 (06/25/04)
selector $\leftarrow$ old_setting ; gf_out(cur_length); gf_string $(0$, make_string $) ;$ decr (str_ptr);
Page D506, lines 8-10 (06/25/04)
METAFONT it says, for example, '(preloaded base=plain 1984.2.29)', showing the year, month, and day that the base file was created. We have base_ident $=0$ before METAFONT's tables are loaded.

Page D514, line 14 from the bottom
(06/25/04)
CMMF, should also be provided for commonly used bases such as cmbase.
Page E1, line 3 (01/06/06)

Zillions of alphabets can be generated by the programs in this book. All
Page E6, lines 16-19 (12/29/04)

- square_dots tells whether dots should be square, not rounded;
- hefty tells whether weight-reducing strategies should be used;
- monospace tells whether the characters should all be forced to have the same width;


## Page E7, line 11

(12/21/02)
hair, vair, stem, curve, ess, flare, dot_size, bar, slab,
Page E7, line $14 \quad(12 / 21 / 02)$
crisp, tiny, fine;
and thin_join should not be less than fine.

| Page E19, line 19 |  |  |  |  | $(11 / 07 / 01)$ |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| cap_notch_cut | $46 / 36$ | $31 / 36$ | $25 / 36$ | $24 / 36$ | $22 / 36$ | $25 / 36$ |

Page E41, line 8
(12/21/02)
extra_endchar $\leftarrow$ extra_endchar \& "charcode $:=c h a r c o d e+c o d e \_o f f s e t ; " ;$
Page E53, line $7 \quad(12 / 21 / 02)$
numeric mid_thickness; mid_thickness $=$ Vround $1 / 3[$ vair, stem $] ;$

Page E125, line 6 from the bottom
(07/10/05)
top $y_{1}=$ top $y_{6}=h ; z_{2}=.5\left[z_{3}, z_{1}\right]+$ bend $;$
Page E125, line 3 from the bottom
(07/10/05)
draw $z_{1}$ - flourish_change $\{u p\}+(0, .15$ asc_height $)\{u p\}$
$\ldots\{\operatorname{right}\}\left(z_{1}+(2 u, 0)\right)---z_{6} \ldots\{$ down $\} z_{7} ;$ \% upper bar
Page E146, also pages 164 and 540
(02/08/03)
[The labels on the new illustrations of beta, omega, and spadesuit are too large, and the resolution of the shapes is too small.]

Page E147, line 11 from the bottom
(04/23/04)
$x_{0}=x_{1}=x_{9} ;$ lft $x_{0 r}=\operatorname{hround}(1.5 u-.5$ hair $) ; x_{2}=x_{4}=x_{6}=x_{8}=.5 w-.25 u ;$
Page E147, line 8 from the bottom
(04/23/04)
$y_{5}=.5\left[y_{4}, y_{6}\right] ;$ top $y_{6 r}-$ bot $y_{4 r}=v s t e m+e p s ;$ bot $y_{8 r}=-o o ; y_{7}=y_{9}=.55\left[y_{6}, y_{8}\right] ;$
Page E149, line 8 from the bottom
(04/23/04)
$y_{5}+.1 x_{\text {_height }}=y_{7}=.5\left[y_{6}, y_{8}\right] ;$ bot $y_{6 r}=-o o$;
Page E157, line 11
(02/29/08)
filldraw $z_{1 l}--z_{2 l} \ldots\left(x_{3}, y_{2 l}\right) \ldots z--z_{1 r}-$ cycle; $\quad \%$ stem

## Page E161, line 7 from the bottom

(04/23/04)
top $y_{1 r}=x_{-}$height $+o o ; y_{2}=y_{4}=.5\left[y_{1}, y_{3}\right] ;$ bot $y_{3 r}=-o o$;
Page E209, line 3
(12/29/04)
\% This lowercase italic alphabet was prepared by D. E. Knuth in December, 1979,
Page E377, lines 3 and 4 from the bottom
(12/22/02)
path $p_{-} ; p_{-}=z_{\$ \$ l}\left\{z_{@ 1}-z_{\$ \$ l}\right\} \ldots$ darkness $\left[z_{@ 1}, .5\left[z_{@ 2}, z_{\$ \$ l}\right]\right] \ldots z_{@ 2}$
$---z_{\S l}--z_{\$_{r}}--z_{@ 0}--z_{\$ \$_{r}}-$ - cycle;
if $\left(y_{\$ \$}>y_{\S}\right) \neq\left(\right.$ ypart precontrol 1 of $p_{-}>$ypart postcontrol 1 of $\left.p_{-}\right)$:
$p_{-}=z_{\$ \$ l}\left\{z_{@ 1}-z_{\$ \$ l}\right\} \ldots$ darkness $\left[z_{@ 1}, .5\left[z_{@ 2}, z_{\$ \$ l}\right]\right]$
$--z_{\$ l}--z_{\S_{r}}--z_{@ 0}--z_{\$ \$ r}--$ cycle; fi
filldraw $p_{-}$; $\%$ arm and beak

Page E379, lines 17 and 18 become one line
(01/06/14)
else: $r t x_{6 r}=\operatorname{hround}(w-1.5 u) ; y_{6}=y_{5 l}+e p s ; \mathbf{f i}$

| Page E379, bottom line of the program | $(01 / 06 / 14)$ |
| :--- | :--- |

math_fit $\left(0, i c^{\#}-2.5 u^{\#}\right)$; penlabels $(0,1,2,3,4,5,6,7)$; endchar;
Page E489, bottom line $\quad(06 / 25 / 04)$
labels( $1,2,3,4,5,6$ ); endchar;
[Labels ' 5 ' and ' 6 ' should also be added to the lower illustration on page E488.]
Page E545, line 11 from the bottom (12/29/04)

The most important general routine in cmbase is probably the pos
Page E551, line 3 from the bottom
(12/29/04)
quantities needed in the calu programs are also established at this time.

| Page E577, right column | $(12 / 23 / 02)$ |
| :--- | :---: |
| $p_{-}, 305,377$. |  |
| padded, 103-111, 117-121, $\underline{549}$. |  |

Page E578, left column
(12/23/02)
postcontrol, 347, 377
precontrol, 347, 377.

